

# Sample Question Paper - 4

CLASS: XII

Session: 2021-22

Mathematics (Code-041)

Term - 1

Time Allowed: 1 hour and 30 minutes

Maximum Marks: 40

## General Instructions:

1. This question paper contains three sections – A, B and C. Each part is compulsory.
2. Section - A has 20 MCQs, attempt any 16 out of 20. 3
3. . Section - B has 20 MCQs, attempt any 16 out of 20
4. Section - C has 10 MCQs, attempt any 8 out of 10.
5. There is no negative marking.
6. All questions carry equal marks.

### SECTION – A

Attempt any 16 questions

1. Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be defined by  $f(x) = \begin{cases} 2x : x > 3 \\ x^2 : 1 < x \leq 3 \\ 3x : x \leq 1 \end{cases}$  [1]  
Then  $f(-1) + f(2) + f(4)$  is  
a) 5 b) 9  
c) none of these d) 14
2. Corner points of the feasible region for an LPP are (0, 2), (3, 0), (6, 0), (6, 8) and (0, 5). Let  $F = 4x + 6y$  be the objective function. Maximum of  $F$  – Minimum of  $F =$  [1]  
a) 48 b) 60  
c) 42 d) 18
3. Find the value of  $b$  for which the function  $f(x) = \begin{cases} 5x - 4 & , 0 < x \leq 1 \\ 4x^2 + 3bx & , 1 < x < 2 \end{cases}$  is continuous [1]  
at every point of its domain, is  
a)  $\frac{13}{3}$  b) -1  
c) 1 d) 0
4. Let  $A$  be a non-singular square matrix of order  $3 \times 3$ . Then  $|\text{adj } A|$  is equal to [1]  
a)  $|A|$  b)  $3|A|$   
c)  $|A|^3$  d)  $|A|^2$
5. A fruit grower can use two types of fertilizer in his garden, brand P and brand Q. The amounts (in kg) of nitrogen, phosphoric acid, potash, and chlorine in a bag of each brand are given in [1]



the table. Tests indicate that the garden needs at least 240 kg of phosphoric acid, at least 270 kg of potash and at most 310 kg of chlorine.

Kg per bag		
	Brand P	Brand Q
Nitrogen	3	3.5
Phosphoric acid	1	2
Potash	3	1.5
Chlorine	1.5	2

If the grower wants to maximise the amount of nitrogen added to the garden, how many bags of each brand should be added? What is the maximum amount of nitrogen added?

- a) 150 bags of brand P and 50 bags of brand Q; Maximum amount of nitrogen = 625 kg
- b) 140 bags of brand P and 50 bags of brand Q; Maximum amount of nitrogen = 595 kg
- c) 160 bags of brand P and 52 bags of brand Q; Maximum amount of nitrogen = 635 kg
- d) 145 bags of brand P and 55 bags of brand Q; Maximum amount of nitrogen = 555 kg

6. The equation of normal to the curve  $3x^2 - y^2 = 8$  which is parallel to the line  $x + 3y = 8$  is [1]

- a)  $3x + y + 8 = 0$
- b)  $x + 3y = 0$
- c)  $3x - y = 8$
- d)  $x + 3y \pm 8 = 0$

7. If  $\omega$  is a complex cube root of unity then the value of  $\begin{vmatrix} 1 & \omega & 1 + \omega \\ 1 + \omega & 1 & \omega \\ \omega & 1 + \omega & 1 \end{vmatrix}$  is [1]

- a) 2
- b) 0
- c) 4
- d) -3

8. If  $y = x^2 \sin \frac{1}{x}$  then  $\frac{dy}{dx} = ?$  [1]

- a)  $-\cos \frac{1}{x} + 2x \sin \frac{1}{x}$
- b)  $-x \sin \frac{1}{x} + \cos \frac{1}{x}$
- c)  $-\cos \frac{1}{x} + x \sin \frac{1}{x}$
- d) none of these

9. Determine the maximum value of  $Z = 11x + 7y$  subject to the constraints  $2x + y \leq 6$ ,  $x \leq 2$ ,  $x \geq 0$ ,  $y \geq 0$ . [1]

- a) 47
- b) 43
- c) 42
- d) 45

10. If  $A = \begin{bmatrix} 0 & 2 & -3 \\ -2 & 0 & -1 \\ 3 & 1 & 0 \end{bmatrix}$  then A is a [1]

- a) skew-symmetric matrix
- b) symmetric matrix
- c) none of these
- d) diagonal matrix

[1]



11. If  $f(x) = \begin{cases} mx + 1, & \text{if } x \leq \frac{\pi}{2} \\ \sin x + n, & \text{if } x > \frac{\pi}{2} \end{cases}$  is continuous at  $x = \frac{\pi}{2}$  then

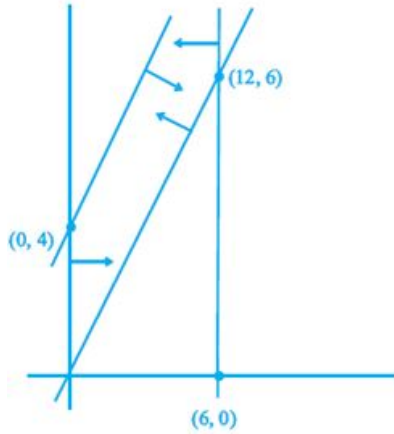
a)  $m = n = \frac{\pi}{2}$

b)  $n = \frac{m\pi}{2}$

c)  $m = 1, n = 0$

d)  $m = \frac{n\pi}{2} + 1$

12. The feasible region for an LPP is shown in the Figure. Let  $F = 3x - 4y$  be the objective function. [1]  
Maximum value of  $F$  is.



a) -18

b) 0

c) 8

d) 12

13. The value of  $k$  for which  $f(x) = \begin{cases} \frac{\sin 5x}{3x}, & \text{if } x \neq 0 \\ k, & \text{if } x = 0 \end{cases}$  is continuous at  $x = 0$  is [1]

a)  $\frac{5}{3}$

b)  $\frac{3}{5}$

c) 0

d)  $\frac{1}{3}$

14. The function  $f(x) = \frac{4-x^2}{4x-x^3}$  is [1]

a) none of these

b) discontinuous at only one point

c) discontinuous at exactly two points

d) discontinuous at exactly three points

15. If  $y = x^{n-1} \log x$  then  $x^2 y_2 + (3 - 2n) xy_1$  is equal to [1]

a)  $n^2 y$

b)  $(n-1)^2 y$

c)  $-n^2 y$

d)  $-(n-1)^2 y$

16. The function  $f(x) = \tan x - x$  [1]

a) always increases

b) never increases

c) always decreases

d) sometimes increases and sometimes decreases.

17. The point on the curve  $y^2 = 4x$  which is nearest to the point (2,1) is [1]

a)  $(1, 2\sqrt{2})$

b)  $(-2, 1)$

c)  $(1, -2)$

d)  $(1, 2)$

18.  $\sin^{-1}\left(\frac{-1}{2}\right) + 2 \cos^{-1}\left(\frac{-\sqrt{3}}{2}\right) = ?$  [1]

a)  $\frac{3\pi}{2}$

b)  $\pi$

c) None of these

d)  $\frac{\pi}{2}$

19. If  $x^y = e^{x-y}$ , then  $\frac{dy}{dx}$  is [1]

a)  $\frac{1-\log x}{1+\log x}$

b)  $\frac{1+x}{1+\log x}$

c)  $\frac{\log x}{(1+\log x)^2}$

d) not defined

20. The curves  $x = y^2$  and  $xy = k$  cut orthogonally when [1]

a)  $6k^2 = 1$

b) None of these

c)  $4k^2 = 1$

d)  $8k^2 = 1$

### SECTION – B

Attempt any 16 questions

21. Let T be the set of all triangles in the Euclidean plane, and let a relation R on T be defined as  $aRb$  if a is congruent to b,  $a, b \in T$ . Then R is [1]

a) an equivalence relation

b) neither reflexive nor symmetric

c) transitive but not symmetric

d) reflexive but not transitive

22.  $f(x) = \sin x \sqrt{3} \cos x$  is maximum when  $x =$  [1]

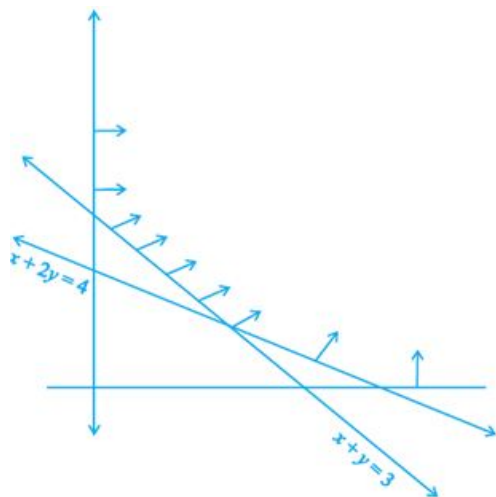
a)  $\frac{\pi}{6}$

b)  $\frac{\pi}{4}$

c) 0

d)  $\frac{\pi}{3}$

23. The feasible region for a LPP is shown in Figure. Evaluate  $Z = 4x + y$  at each of the corner points of this region. Find the minimum value of Z, if it exists [1]



a) Minimum value = 2

b) Minimum value = 5

c) Minimum value = 4

d) Minimum value = 3

24. The slope of the tangent to the curve  $x = 3t^2 + 1$ ,  $y = t^3 - 1$  at  $x = 1$  is [1]

a)  $\frac{1}{2}$

b)  $\infty$

c) 0

d) -2

25. If,  $y = \frac{1}{1+x^{a-b}+x^{c-b}} + \frac{1}{1+x^{b-c}+x^{a-c}} + \frac{1}{1+x^{b-a}+x^{c-a}}$ , then  $\frac{dy}{dx}$  is equal to [1]

- a) 1  
c) none of these
26.  $\cot(\tan^{-1}x + \cot^{-1}x)$ . [1]  
a) 1  
b)  $1/2$   
c) 0  
d) None of these
27. If the set A contains 5 elements and the set B contains 6 elements, then the number of one – one and onto mappings from A to B is [1]  
a) none of these  
b) 720  
c) 120  
d) 0
28.  $\tan [2 \tan^{-1} \frac{1}{5} - \frac{\pi}{4}] = ?$  [1]  
a)  $\frac{7}{12}$   
b)  $\frac{7}{17}$   
c)  $\frac{-7}{12}$   
d)  $\frac{-7}{17}$
29. If  $y = \tan^{-1} \left( \frac{\sqrt{a} + \sqrt{x}}{1 - \sqrt{ax}} \right)$  then  $\frac{dy}{dx} = ?$  [1]  
a)  $\frac{2}{\sqrt{x}(1+x)}$   
b)  $\frac{1}{(1+x)}$   
c)  $\frac{1}{2\sqrt{x}(1+x)}$   
d)  $\frac{1}{\sqrt{x}(1+x)}$
30. If A' is the transpose of a square matrix A, then [1]  
a)  $|A| + |A'| = 0$   
b)  $|A| = |A'|$   
c)  $|A| \neq |A'|$   
d) None of these
31. If  $\sqrt{1-x^6} + \sqrt{1-y^6} = a^3(x^3 - y^3)$ , then  $\frac{dy}{dx}$  is equal to [1]  
a)  $\frac{y^2}{x^2} \sqrt{\frac{1-y^6}{1-x^6}}$   
b)  $\frac{x^2}{y^2} \sqrt{\frac{1-y^6}{1-x^6}}$   
c)  $\frac{x^2}{y^2} \sqrt{\frac{1-x^6}{1-y^6}}$   
d) none of these
32. If  $y = \frac{e^x - e^{-x}}{e^x + e^{-x}}$ , then  $\frac{dy}{dx}$  is equal to [1]  
a)  $1 + y^2$   
b) None of these  
c)  $1 - y^2$   
d)  $y^2 + 1$
33. If the function  $f(x) = 2x^2 - kx + 5$  is increasing on  $(1, 2)$ , then k lies in the interval [1]  
a)  $(4, \infty)$   
b)  $(-\infty, 8)$   
c)  $(8, \infty)$   
d)  $(-\infty, 4)$
34.  $\sin(\tan^{-1} x)$ ,  $|x| < 1$  is equal to [1]  
a)  $\frac{1}{\sqrt{1+x^2}}$   
b)  $\frac{x}{\sqrt{1+x^2}}$   
c)  $\frac{x}{\sqrt{1-x^2}}$   
d)  $\frac{1}{\sqrt{1-x^2}}$

[1]



35. 
$$\begin{vmatrix} b+c & a & a \\ b & c+a & b \\ c & c & a+b \end{vmatrix} = ?$$

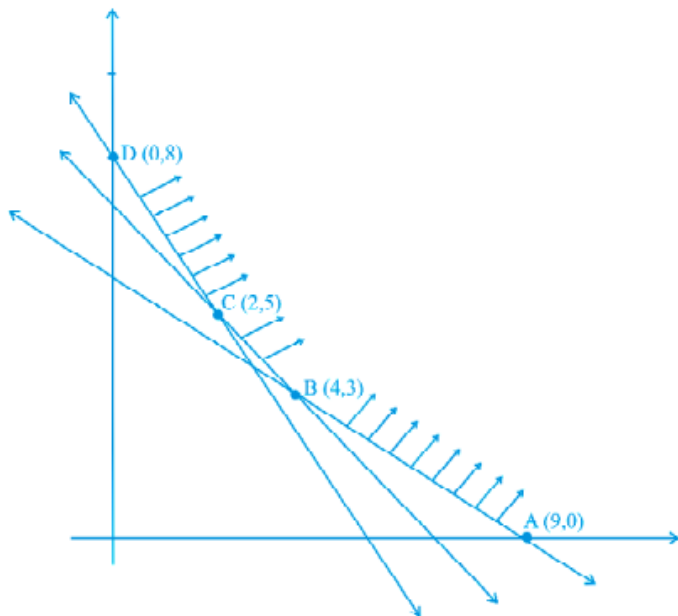
a)  $2(a+b+c)$

b)  $4abc$

c)  $(ab+bc+ca)$

d) None of these

36. Feasible region (shaded) for a LPP is shown in the Figure. Minimum of  $Z = 4x + 3y$  occurs at the point [1]



a)  $(4, 3)$

b)  $(9, 0)$

c)  $(0, 8)$

d)  $(2, 5)$

37. If  $A$  is an invertible matrix of order 2, then  $\det(A^{-1})$  is equal to [1]

a) 0

b)  $\frac{1}{\det(A)}$

c)  $\det(A)$

d) 1

38. Let  $f(x) = x^3$ , then  $f(x)$  has a [1]

a) point of inflexion at  $x = 0$

b) local maxima at  $x = 0$

c) none of these

d) local minima at  $x = 0$

39. If  $f(x) = \sqrt{1 - \sqrt{1 - x^2}}$ , then  $f(x)$  is [1]

a) none of these

b) continuous on  $[-1, 1]$  and differentiable on  $(-1, 1)$

c) continuous on  $[-1, 1]$  and differentiable on  $(-1, 0) \cup (0, 1)$

d) continuous and differentiable on  $[-1, 1]$

40. Which of the following functions from  $\mathbb{Z}$  into  $\mathbb{Z}$  are bijections? [1]

a)  $f(x) = x^3$

b)  $f(x) = 2x + 1$

c)  $f(x) = x + 2$

d)  $f(x) = x^2 + 1$

## SECTION - C

**Attempt any 8 questions**

41. If  $\tan^{-1} \left\{ \frac{\sqrt{1+x^2} - \sqrt{1-x^2}}{\sqrt{1+x^2} + \sqrt{1-x^2}} \right\} = \alpha$ , then  $x^2 =$  [1]
- a)  $\cos \alpha$  b)  $\sin 2\alpha$
- c)  $\cos 2\alpha$  d)  $\sin \alpha$
42. Maximize  $Z = -x + 2y$ , subject to the constraints:  $x \geq 3$ ,  $x + y \geq 5$ ,  $x + 2y \geq 6$ ,  $y \geq 0$ . [1]
- a) Z has no maximum value b) Maximum  $Z = 14$  at  $(2, 6)$
- c) Maximum  $Z = 12$  at  $(2, 6)$  d) Maximum  $Z = 10$  at  $(2, 6)$
43. If  $f$  is derivable at  $x = a$ , then  $\lim_{x \rightarrow a} \frac{xf(a) - af(x)}{x - a}$  is equal to [1]
- a)  $af'(9a) - f(a)$  b)  $f(a) - af'(a)$
- c)  $f'(a)$  d) None of these
44. If  $A, B$  are two  $n \times n$  non-singular matrices, then what can you infer about  $AB$ ? [1]
- a)  $AB$  is singular b)  $(AB)^{-1}$  does not exist
- c)  $AB$  is non-singular d)  $(AB)^{-1} = A^{-1}B^{-1}$
45. Let  $S$  be the set of all real numbers and let  $R$  be a relation on  $S$ , defined by  $aRb \Leftrightarrow (1 + ab) > 0$ . [1]  
Then,  $R$  is
- a) None of these b) Reflexive and transitive but not symmetric
- c) Symmetric and transitive but not reflexive d) reflexive and symmetric but not transitive

**Question No. 46 to 50 are based on the given text. Read the text carefully and answer the questions:**

Consider 2 families A and B. Suppose there are 4 men, 4 women and 4 children in family A and 2 men, 2 women and 2 children in family B. The recommended daily amount of calories is 2400 for a man, 1900 for a woman, 1800 for children and 45 grams of proteins for a man, 55 grams for a woman and 33 grams for children.



46. The requirement of calories and proteins for each person in matrix form can be represented as
- a)  $\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$  b)  $\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$

	<i>Calories</i>	<i>Proteins</i>
<i>Man</i>	2400	45
<i>Woman</i>	1900	55
<i>Children</i>	1800	33

	<i>Calories</i>	<i>Proteins</i>
<i>Man</i>	1900	55
<i>Woman</i>	2400	45
<i>Children</i>	1800	33

c)

	<i>Calories</i>	<i>Proteins</i>
<i>Man</i>	1800	33
<i>Woman</i>	1900	55
<i>Children</i>	2400	45

d)

	<i>Calories</i>	<i>Proteins</i>
<i>Man</i>	2400	33
<i>Woman</i>	1900	55
<i>Children</i>	1800	45

47. The requirement of calories of family A is [1]
- a) 15800 b) 15000
- c) 24000 d) 24400
48. The requirement of proteins for family B is [1]
- a) 266 grams b) 300 grams
- c) 332 grams d) 560 grams
49. If A and B are two matrices such that  $AB = B$  and  $BA = A$ , then  $A^2 + B^2$  equals [1]
- a)  $A + B$  b)  $2BA$
- c)  $2AB$  d)  $AB$
50. If  $A = (a_{ij})_{m \times n}$ ,  $B = (b_{ij})_{n \times p}$  and  $C = (c_{ij})_{p \times q}$ , then the product  $(BC)A$  is possible only when [1]
- a)  $p = q$  b)  $m = q$
- c)  $n = q$  d)  $m = p$

# Solution

## SECTION – A

1. (b) 9

**Explanation:** Given that,

$$f(x) = \begin{cases} 2x : x > 3 \\ x^2 : 1 < x \leq 3 \\ 3x^2 : x \leq 1 \end{cases}$$

Now,

$$f(-1) = 3(-1) = -3 \text{ [since } -1 < 1 \text{ and } f(x) = 3x \text{ for } x \leq 1]$$

$$f(2) = 2^2 = 4 \text{ [since } 2 < 3 \text{ and } f(x) = x^2 \text{ for } 1 < x \leq 3]$$

$$f(4) = 2(4) = 8 \text{ [since } 4 > 3 \text{ and } f(x) = 2x \text{ for } x > 3]$$

$$\therefore f(-1) + f(2) + f(4) = -3 + 4 + 8 = 9$$

2. (b) 60

**Explanation:** Here the objective function is given by :  $F = 4x + 6y$ .

Corner points	$Z = 4x + 6y$
(0, 2)	12(Min.)
(3, 0)	12.(Min.)
(6, 0)	24
(6, 8)	72
(0, 5)	30

Maximum of  $F$  – Minimum of  $F = 72 - 12 = 30$ .

3. (b) -1

**Explanation:**  $\lim_{x \rightarrow 1^-} f(x) = \lim_{x \rightarrow 1^+} f(x)$

$$\lim_{x \rightarrow 1} 5x - 4 = \lim_{x \rightarrow 1} 4x^2 + 36x$$

$$5 - 4 = 4 + 3b$$

$$1 = 4 + 3b$$

$$b = -1$$

4. (d)  $|A|^2$

**Explanation:** For a square matrix of order  $n \times n$ ,

$$\text{We know that } A \cdot \text{adj}A = |A|I$$

Here,  $n=3$

$$\therefore |A \cdot \text{adj}A| = |A|^n$$

$$|\text{adj}A| = |A|^{n-1}$$

$$\text{So, } |A \cdot \text{adj}A| = |A|^{3-1} = |A|^2$$

5. (b) 140 bags of brand P and 50 bags of brand Q; Maximum amount of nitrogen = 595 kg

**Explanation:** Let the number of bags used for fertilizer of brand P =  $x$  And the number of bags used for fertilizer of brand Q =  $y$ . Here,  $Z = 3x + 3.5y$  subject to constraints :  $1.5x + 2y \leq 310$ ,  $x + 2y \geq 240$ ,  $3x + 1.5y \geq 270$ ,  $x, y \geq 0$

Corner points	$Z = 3x + 3.5y$
C(40, 100)	470.....(Min.)
B (140, 50)	595.....(Max.)
D(20, 140)	550



Here  $Z = 595$  is maximum i.e. 140 bags of brand P and 50 bags of brand Q; Maximum amount of nitrogen = 595 kg.

6. (d)  $x + 3y \pm 8 = 0$

**Explanation:** Given equation of the curve is

$$3x^2 - y^2 = 5 \dots (i)$$

Differentiating both sides w.r.t, we get

$$6x - 2y \frac{dy}{dx} = 0$$

$$\Rightarrow \frac{dy}{dx} = \frac{3x}{y}, \text{ which is slope of tangent at any point on the curve}$$

$$\Rightarrow \text{slope of normal at any point on the curve is } -\frac{dx}{dy} = \frac{-y}{3x}$$

$$\therefore -\frac{y}{3x} = -\frac{1}{3}$$

$$\Rightarrow y = x \dots (ii)$$

From (i) and (ii), we get

$$3x^2 - x^2 = 8$$

$$\Rightarrow x^2 = 4$$

$$\Rightarrow x = \pm 2$$

For  $x = 2$ ,  $y = 2$  [using (ii)]

and for  $x = -2$ ,  $y = -2$  [using (ii)]

Thus, the points on the curve at which normal to the curve are parallel to the line  $x + 3y$  are  $(2, 2)$  and  $(-2, -2)$ .

$\therefore$  Required equations of normal are

$$y - 2 = -\frac{1}{3}(x - 2) \text{ and } y + 2 = -\frac{1}{3}(x + 2)$$

$$\text{or } 3y + x = 8 \text{ and } 3y + x = -8$$

7. (c) 4

**Explanation:**  $1 + \omega + \omega^2 = 0 \Rightarrow (1 + \omega) = -\omega^2$ . Put  $(1 + \omega) = -\omega^2$  and expand.

8. (a)  $-\cos \frac{1}{x} + 2x \sin \frac{1}{x}$

**Explanation:** Given that  $y = x^2 \sin \frac{1}{x}$

Differentiating with respect to  $x$ , we obtain

$$\frac{dy}{dx} = x^2 \cos \frac{1}{x} \times -\frac{1}{x^2} + 2x \sin \frac{1}{x} = 2x \sin \frac{1}{x} - \cos \frac{1}{x}$$

9. (c) 42

**Explanation:** Here, maximize  $Z = 11x + 7y$ , subject to the constraints:  $2x + y \leq 6$ ,  $x \leq 2$ ,  $x \geq 0$ ,  $y \geq 0$ .

Corner points	$Z = 11x + 7y$
$C(0, 0)$	0
$B(2, 0)$	22
$D(2, 2)$	36
$A(0, 6)$	42

Hence the maximum value is 42

10. (a) skew-symmetric matrix

**Explanation:** The diagonal elements of a skew-symmetric matrix is always zero and the elements  $a_{ij} = -a_{ji}$ .

11. (b)  $n = \frac{m\pi}{2}$

**Explanation:** We have,  $f(x) = \begin{cases} mx + 1, & \text{if } x \leq \frac{\pi}{2} \\ \sin x + n, & \text{if } x > \frac{\pi}{2} \end{cases}$  is continuous at  $x = \frac{\pi}{2}$

$$\therefore LHL = \lim_{x \rightarrow \frac{\pi}{2}} (mx + 1) = \lim_{h \rightarrow 0} [m(\frac{\pi}{2} - h) + 1] = \frac{m\pi}{2} + 1$$



$$\text{and } RHL = \lim_{x \rightarrow \frac{\pi}{2}} (\sin x + n) = \lim_{h \rightarrow \infty} \left[ \sin\left(\frac{\pi}{2} + h\right) + n \right]$$

$$= \lim_{n \rightarrow 0} \cos h + n = 1 + n$$

Since the function is continuous, we have

$$LHL = RHL$$

$$\Rightarrow m \cdot \frac{\pi}{2} + 1 = n + 1$$

$$\therefore n = m \cdot \frac{\pi}{2}$$

12. (d) 12

**Explanation:**

Corner points	Z = 3x - 4y
(0, 0)	0
(0,4)	-16
(12,6)	12.....(Max.)

13. (a)  $\frac{5}{3}$

**Explanation:** Since f(x) is continuous on 0, then we

$$\Rightarrow \lim_{x \rightarrow 0} \frac{\sin 5x}{3x} = f(0)$$

$$\Rightarrow \lim_{x \rightarrow 0} \frac{\sin 5x}{3x} \times \frac{5x}{5x} = f(0)$$

$$\Rightarrow \lim_{x \rightarrow 0} \frac{\sin 5x}{5x} \times \frac{5x}{3x} = f(0)$$

$$\Rightarrow f(0) = \frac{5}{3}$$

$$\Rightarrow k = \frac{5}{3}$$

14. (d) discontinuous at exactly three points

**Explanation:** We have,  $f(x) = \frac{4-x^2}{4x-x^3} = \frac{(4-x^2)}{x(4-x^2)}$

$$= \frac{(4-x^2)}{x(2^2-x^2)} = \frac{4-x^2}{x(2+x)(2-x)}$$

Clearly, f(x) is discontinuous at exactly three points x = 0, x = -2 and x = 2.

15. (a)  $n^2y$

**Explanation:**  $y = x^{n-1} \log x$

Differentiating both sides w.r.t. to x we get,

$$y_1 = x^{n-2} + (n-1) x^{n-2} \log x$$

$$xy_1 = x^{n-1} + (n-1) x^{n-1} \log x$$

$$= x^{n-1} + (n-1) y$$

Again differentiating both sides w.r.t. to x we get,

$$xy_2 + y_1 = (n-1) x^{n-2} + (n-1) y_1$$

$$\Rightarrow x^2 y_2 + xy_1 - x(n-1) y_1 = (n-1) x^{n-1}$$

$$\Rightarrow x^2 y_2 + xy_1 (1 + 1 - n) = (n-1) (xy_1 - (n-1) y)$$

$$\Rightarrow x^2 y_2 + xy_1 (2 - n + 1 - n) = -(n-1)^2 y$$

$$\Rightarrow x^2 y_2 + xy_1 (3 - 2n) = -(n-1)^2 y$$

16. (a) always increases

**Explanation:** We have,  $f(x) = \tan x - x$

$$\therefore f'(x) = \sec^2 x - 1$$

$$\Rightarrow f'(x) \geq 0, \forall x \in R$$

So, f(x) always increases

17. (d) (1, 2)

**Explanation:**  $y^2 = 4x \Rightarrow x = \frac{y^2}{4}$

$$\Rightarrow d = \sqrt{(x-2)^2 + (y-1)^2}$$

$$\Rightarrow d^2 = (x-2)^2 + (y-1)^2$$

$$\Rightarrow d^2 = \left(\frac{y^2}{4} - 2\right)^2 + (y-1)^2$$

$$\text{Let } u = \left(\frac{y^2}{4} - 2\right)^2 + (y-1)^2$$

$$\Rightarrow \frac{du}{dy} = 2\left(\frac{y^2}{4} - 2\right) \frac{y}{2} + 2(y-1)$$

To find minima

$$\frac{du}{dy} = 0$$

$$2\left(\frac{y^2}{4} - 2\right) \frac{y}{2} + 2(y-1) = 0$$

$$\Rightarrow y = 2 \Rightarrow x = 1 \left(x = \frac{y^2}{4}\right)$$

$$\frac{d^2u}{dy^2} = \frac{3y^2}{4}$$

$$\Rightarrow \left(\frac{d^2u}{dy^2}\right)_{(1,2)} = 3 > 0$$

Hence, nearest point is (1, 2).

18. (a)  $\frac{3\pi}{2}$

**Explanation:** Given:  $\sin^{-1}\left(\frac{-1}{2}\right) + 2 \cos^{-1}\left(\frac{-\sqrt{3}}{2}\right)$

Let,  $x = \sin^{-1}\left(\frac{-1}{2}\right) + 2 \cos^{-1}\left(\frac{-\sqrt{3}}{2}\right)$

$$\Rightarrow x = -\sin^{-1}\left(\frac{1}{2}\right) + 2 \left[\pi - \cos^{-1}\left(\frac{\sqrt{3}}{2}\right)\right] \quad (\because \sin^{-1}(-\theta) = -\sin^{-1}(\theta) \text{ and } \cos^{-1}(-\theta) = \pi - \cos^{-1}(\theta))$$

$$\Rightarrow x = -\left(\frac{\pi}{6}\right) + 2 \left[\pi - \frac{\pi}{6}\right]$$

$$\Rightarrow x = -\left(\frac{\pi}{6}\right) + 2 \left[\frac{5\pi}{6}\right]$$

$$\Rightarrow x = -\frac{\pi}{6} + \frac{5\pi}{3}$$

$$\Rightarrow x = \frac{3\pi}{2}$$

19. (c)  $\frac{\log x}{(1+\log x)^2}$

**Explanation:**  $x^y = e^{x \cdot y}$

Taking log on both sides,

$$\log x^y = \log e^{x \cdot y}$$

$$y \log x = x \cdot y$$

$$y \log x + y = x$$

$$y = \frac{x}{\log x + 1}$$

Differentiate with respect to x,

$$\frac{dy}{dx} = \frac{(\log x + 1) - x \times \frac{1}{x}}{(\log x + 1)^2}$$

$$\frac{dy}{dx} = \frac{(\log x + 1) - 1}{(\log x + 1)^2}$$

$$\frac{dy}{dx} = \frac{\log x}{(\log x + 1)^2}$$

20. (d)  $8k^2 = 1$

**Explanation:** Let  $(\alpha, \beta)$  be the point of intersection of the given curves

$$\text{Now, } x = y^2 \Rightarrow 2y \frac{dy}{dx} = 1 \Rightarrow \frac{dy}{dx} = \frac{1}{2y} \dots (i)$$

$$xy = k \Rightarrow x \cdot \frac{dy}{dx} + y = 0 \Rightarrow \frac{dy}{dx} = \frac{-y}{x} \dots (ii)$$

$$m_1 = \left(\frac{dy}{dx}\right)_{(\alpha, \beta)} = \left(\frac{1}{2y}\right)_{(\alpha, \beta)} = \frac{1}{2\beta}, m_2 = \left(\frac{dy}{dx}\right)_{(\alpha, \beta)} = \left(\frac{-y}{x}\right)_{(\alpha, \beta)} = \frac{-\beta}{\alpha}$$

Two curves cut orthogonally means  $m_1 \cdot m_2 = -1$

$$\Rightarrow \frac{1}{2\beta} \cdot \frac{-\beta}{\alpha} = -1 \Rightarrow 2\alpha = 1 \Rightarrow \alpha = \frac{1}{2} \dots (iii)$$

Since  $(\alpha, \beta)$  lies on  $x = y^2$  we have  $\alpha = \beta^2 \Rightarrow \beta^2 = \frac{1}{2} \dots (iv)$   
 Also, Since,  $(\alpha, \beta)$  lies on  $xy = k$ , we get  $\alpha \cdot \beta = k \Rightarrow k^2 = \alpha^2 \cdot \beta^2$   
 $\Rightarrow k^2 = \frac{1}{4} \cdot \frac{1}{2} = \frac{1}{8}$  from (iii) and (iv)  
 $\Rightarrow 8k^2 = 1$

## SECTION – B

21. (a) an equivalence relation

**Explanation:** Let T be the set of all triangles in the Euclidean plane with R, a relation in T is given by  $R = \{(T_1, T_2): T_1 \text{ is congruent to } T_2\}$

$(T_1, T_2) \in R$  if  $T_1$  is congruent to  $T_2$ .

**Reflexivity:**  $T_1 \cong T_1 \Rightarrow (T_1, T_1) \in R$ .

**Symmetry:**  $(T_1, T_2) \in R \Rightarrow T_1 \cong T_2 \Rightarrow T_2 \cong T_1 \Rightarrow (T_2, T_1) \in R$ .

**Transitivity:**  $(T_1, T_2) \in R$  and  $(T_2, T_3) \in R$ .

$\Rightarrow T_1 \cong T_2$  and  $T_2 \cong T_3 \Rightarrow T_1 \cong T_3 \Rightarrow (T_1, T_3) \in R$ .

Therefore, R is an equivalence relation.

22. (a)  $\frac{\pi}{6}$

**Explanation:**  $f(x) = \sin x + \sqrt{3} \cos x$

$\Rightarrow f'(x) = \cos x - \sqrt{3} \sin x$

for maxima or minima

$f'(x) = 0$

$\cos x - \sqrt{3} \sin x = 0$

$\Rightarrow \tan x = \frac{1}{\sqrt{3}} \Rightarrow x = \frac{\pi}{6}$

$f''(x) = -\sin x - \sqrt{3} \cos x$

$\Rightarrow f''\left(\frac{\pi}{6}\right) = -\sin \frac{\pi}{6} - \sqrt{3} \cos \frac{\pi}{6} = \frac{-1-\sqrt{3}}{2} < 0$

function has local maxima at  $x = \frac{\pi}{6}$

23. (a) Minimum value = 2

**Explanation:**

Corner points	$Z = 4x + y$
(0, 2)	2
(0, 3)	3
(2, 1)	9

Hence the minimum value is 2

24. (c) 0

**Explanation:**  $x = 3t^2 + 1$  and  $y = t^3 - 1$

$\frac{dx}{dt} = 6t$  and  $\frac{dy}{dt} = 3t^2$

$\Rightarrow \frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}} = \frac{t}{2} \dots (i)$

But,

$x = 1$

$\Rightarrow 3t^2 + 1 = 1$

$\Rightarrow t = 0$

$\frac{dy}{dx} = \frac{t}{2} = 0$  ( $\because$  From (i))

25. (d) 0

**Explanation:**  $y = \frac{1}{1+x^{a-b}+x^{c-b}} + \frac{1}{1+x^{b-c}+x^{a-c}} + \frac{1}{1+x^{b-a}+x^{c-a}}$

$y = \frac{1}{1+\frac{x^a}{x^b}+\frac{x^c}{x^b}} + \frac{1}{1+\frac{x^b}{x^c}+\frac{x^a}{x^c}} + \frac{1}{1+\frac{x^b}{x^a}+\frac{x^c}{x^a}}$



$$y = \frac{x^b}{x^a + x^b + x^c} + \frac{x^c}{x^a + x^b + x^c} + \frac{x^a}{x^a + x^b + x^c}$$

$$y = \frac{x^a + x^b + x^c}{x^a + x^b + x^c}$$

$$y = 1$$

$$\frac{dy}{dx} = 0$$

26. (c) 0

**Explanation:** Given:  $\cot(\tan^{-1}x + \cot^{-1}x)$

Let,  $x = \cot(\tan^{-1}x + \cot^{-1}x)$

$$x = \cot\left(\frac{\pi}{2}\right) \quad (\because \tan^{-1}x + \cot^{-1}x = \frac{\pi}{2})$$

$$x = 0$$

27. (d) 0

**Explanation:** Because the no. of elements in domain i.e. in A is less than the no. of elements in co-domain i.e. in B. Therefore, no bijection mapping is possible.

28. (d)  $\frac{-7}{17}$

**Explanation:** The given equation is of  $\tan\left[2 \tan^{-1} \frac{1}{5} - \frac{\pi}{4}\right]$

$$\text{Let } \tan\left(2 \tan^{-1} \frac{1}{5} - \frac{\pi}{4}\right) = \tan\left(\tan^{-1} \left(\frac{2\left(\frac{1}{5}\right)}{1 - \left(\frac{1}{5}\right)^2}\right) - \frac{\pi}{4}\right) \quad (\because 2 \tan^{-1} x = \tan^{-1} \left(\frac{2x}{1-x^2}\right))$$

$$= \tan\left(\tan^{-1} \left(\frac{\frac{2}{5}}{1 - \frac{1}{25}}\right) - \frac{\pi}{4}\right)$$

$$= \tan\left(\tan^{-1} \left(\frac{5}{12}\right) - \frac{\pi}{4}\right)$$

$$= \tan\left(\tan^{-1} \left(\frac{5}{12}\right) - \frac{\pi}{4}\right)$$

$$= \tan\left(\tan^{-1} \left(\frac{5}{12}\right) - \tan^{-1}(1)\right) \quad (\because \tan\left(\frac{\pi}{4}\right) = 1)$$

$$= \tan\left(\tan^{-1} \left(\frac{\frac{5}{12} - 1}{1 + \frac{5}{12}}\right)\right) \quad (\tan^{-1} x - \tan^{-1} y = \tan^{-1} \left(\frac{x-y}{1+xy}\right))$$

$$= \tan\left(\tan^{-1} \left(\frac{-7}{17}\right)\right)$$

$$\tan\left(2 \tan^{-1} \frac{1}{5} - \frac{\pi}{4}\right) = \frac{-7}{17}$$

29. (c)  $\frac{1}{2\sqrt{x}(1+x)}$

**Explanation:** Given that  $y = \tan^{-1} \frac{\sqrt{a} + \sqrt{x}}{1 - \sqrt{ax}}$

Let  $\sqrt{a} = \tan A$  and  $\sqrt{x} = \tan B$ , then  $A = \tan^{-1} \sqrt{a}$  and  $B = \tan^{-1} \sqrt{x}$

$$\text{Hence, } y = \tan^{-1} \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

Using  $\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$ , we obtain

$$y = \tan^{-1} \tan(A + B) = A + B$$

$$= \tan^{-1} \sqrt{a} + \tan^{-1} \sqrt{x}$$

Differentiating with respect to x, we obtain

$$\frac{dy}{dx} = 0 + \frac{1}{1 + (\sqrt{x})^2} \times \frac{1}{2\sqrt{x}} = \frac{1}{2\sqrt{x}(1+x)}$$

30. (b)  $|A| = |A'|$

**Explanation:** The determinant of a matrix A and its transpose always same. Because if we interchange the rows into column in a determinant the value of determinant remains unaltered.

31. (b)  $\frac{x^2}{y^2} \sqrt{\frac{1-y^6}{1-x^6}}$

**Explanation:**  $\sqrt{1-x^6} + \sqrt{1-y^6} = a^3(x^3 - y^3)$

$$\text{Put } x^3 = \sin u, y^3 = \sin v$$

$$\Rightarrow \cos u + \cos v = a^3(\sin u - \sin v)$$

$$\Rightarrow 2 \cos\left(\frac{u+v}{2}\right) \cos\left(\frac{u-v}{2}\right) = a^3 \times 2 \cos\left(\frac{u+v}{2}\right) \sin\left(\frac{u-v}{2}\right)$$



$$\Rightarrow \cos\left(\frac{u-v}{2}\right) = \sin\left(\frac{u-v}{2}\right)$$

$$\Rightarrow \frac{u-v}{2} = \tan^{-1} \frac{\pi}{4}$$

$$\Rightarrow u - v = \frac{\pi}{2}$$

$$\Rightarrow \sin^{-1} x^3 + \sin^{-1} y^3 = \frac{\pi}{2}$$

Differentiating with respect to x,

$$\frac{3x^2}{\sqrt{1-x^6}} - \frac{3y^2}{\sqrt{1-y^6}} \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = \frac{x^2}{y^2} \sqrt{\frac{1-y^6}{1-x^6}}$$

32. (c)  $1 - y^2$

**Explanation:** Solution.  $\frac{dy}{dx} = \frac{d}{dx} \left( \frac{e^x - e^{-x}}{e^x + e^{-x}} \right)$

$$= \frac{(e^x + e^{-x})(e^x + e^{-x}) - (e^x - e^{-x})(e^x - e^{-x})}{(e^x + e^{-x})^2} = \frac{(e^x + e^{-x})^2}{(e^x + e^{-x})^2} - \frac{(e^x - e^{-x})^2}{(e^x + e^{-x})^2} = 1 - y^2.$$

Which is the required solution.

33. (d)  $(-\infty, 4)$

**Explanation:**  $f(x) = 2x^2 - kx + 5$

$$f'(x) = 4x - k$$

for f(x) to be increasing, we must have

$$f(x) > 0$$

$$4x - k > 0$$

$$K < 4x$$

$$\text{since } x \in [1, 2], 4x \in [4, 8]$$

so, the minimum value of  $4x$  is 4.

$$\text{since } K < 4x, K < 4.$$

$$k \in (-\infty, 4)$$

34. (b)  $\frac{x}{\sqrt{1+x^2}}$

**Explanation:** Let  $\tan^{-1} x = y$ , then  $\tan y = x \Rightarrow \sin y = \frac{x}{\sqrt{1+x^2}}$

$$\therefore y = \sin^{-1} \left( \frac{x}{\sqrt{1+x^2}} \right)$$

$$\Rightarrow \tan^{-1} x = \sin^{-1} \left( \frac{x}{\sqrt{1+x^2}} \right)$$

$$\Rightarrow \sin(\tan^{-1} x) = \sin \left( \sin^{-1} \left( \frac{x}{\sqrt{1+x^2}} \right) \right)$$

$$= \frac{x}{\sqrt{1+x^2}}$$

35. (b)  $4abc$

**Explanation:** Apply  $R^1 \rightarrow R^1 - (R^2 + R^3)$

Take  $(-2)$  common from  $R_1$ . Apply  $R^2 \rightarrow (R^2 - R^1)$  and  $R^3 \rightarrow (R^3 - R^1)$

36. (d)  $(2, 5)$

**Explanation:**  $Z = 4x + 3y$

$$1. (0, 8) = 24$$

$$2. (2, 5) = 8 + 15 = 23$$

$$3. (4, 3) = 16 + 9 = 25$$

$$4. (9, 0) = 36 + 0 = 36$$

The correct answer is  $(2, 5)$  as it gives the minimum value.

37. (b)  $\frac{1}{\det(A)}$

**Explanation:** We know that,  $A^{-1} = \frac{1}{|A|} \text{Adj}(A)$

$$\text{So, } |A^{-1}| = \left| \frac{1}{|A|} \text{Adj}(A) \right|$$

$$\begin{aligned}
&= \frac{1}{|A|^n} |\text{Adj}(A)| \\
&= \frac{1}{|A|^n} |A|^{n-1} = \frac{1}{|A|^1} \\
&= \frac{1}{|A|^1}
\end{aligned}$$

{since  $\text{adj}(A)$  is of order  $n$  and  $|\text{Adj}(A)| = |A|^{n-1}$ }

38. (a) point of inflexion at  $x = 0$

**Explanation:** Given  $f(x) = x^3$

$$f'(x) = 3x^2$$

For point of inflexion, we have  $f'(x) = 0$

$$f'(x) = 0 \Rightarrow 3x^2 = 0 \Rightarrow x = 0$$

Hence,  $f(x)$  has a point of inflexion at  $x = 0$ .

But  $x = 0$  is not a local extremum as we cannot find an interval  $I$  around  $x = 0$  such that

$$f(0) \geq f(x) \quad \text{or} \quad f(0) \leq f(x) \quad \text{for all } x \in I$$

39. (c) continuous on  $[-1, 1]$  and differentiable on  $(-1, 0) \cup (0, 1)$

**Explanation:** Given that  $f(x) = \sqrt{1 - \sqrt{1 - x^2}}$

So, the function will be defined for those values of  $x$  for which

$$1 - x^2 \geq 0$$

$$\Rightarrow x^2 \leq 1$$

$$\Rightarrow |x| \leq 1$$

$$\Rightarrow -1 \leq x \leq 1$$

$\therefore$  Function is continuous in  $[-1, 1]$ .

Now, we will check the differentiability at  $x = 0$

LHD at  $x = 0$ ,

$$\begin{aligned}
\lim_{x \rightarrow 0^-} \frac{f(x) - f(0)}{x - 0} &= \lim_{h \rightarrow 0} \frac{f(0 - h) - f(0)}{0 - h - 0} \\
&= \lim_{h \rightarrow 0} \frac{\sqrt{1 - \sqrt{1 - (0 - h)^2}} - (0)}{-h} = -\infty
\end{aligned}$$

$\therefore$  LHD does not exist, so  $f(x)$  is not differentiable at  $x = 0$

$\therefore f(x)$  is not differentiable at  $x = 0$ .

40. (c)  $f(x) = x + 2$

**Explanation:** Injectivity: Let  $x, y \in \mathbb{Z}$ , then,  $f(x) = f(y) \Rightarrow x + 2 = y + 2 \Rightarrow x = y \Rightarrow f$  is one-one.

Surjectivity: Let  $f(x) = y$ , where  $y \in \mathbb{Z}$ ,  $\Rightarrow x + 2 = y \Rightarrow x = y - 2 \in \mathbb{Z} \Rightarrow f$  is onto.

Therefore,  $f$  is a bijective function.

## SECTION - C

41. (b)  $\sin 2\alpha$

**Explanation:**  $\tan^{-1} \left( \frac{\sqrt{1+x^2} - \sqrt{1-x^2}}{\sqrt{1+x^2} + \sqrt{1-x^2}} \right) = \alpha$

$$\begin{aligned}
&\Rightarrow \frac{\sqrt{1+x^2} - \sqrt{1-x^2}}{\sqrt{1+x^2} + \sqrt{1-x^2}} = \tan \alpha \\
&\Rightarrow \frac{\sqrt{1+x^2} - \sqrt{1-x^2}}{\sqrt{1+x^2} + \sqrt{1-x^2}} \times \frac{\sqrt{1+x^2} - \sqrt{1-x^2}}{\sqrt{1+x^2} - \sqrt{1-x^2}} = \tan \alpha \\
&\Rightarrow \frac{(\sqrt{1+x^2})^2 + (\sqrt{1-x^2})^2 - 2\sqrt{1+x^2}\sqrt{1-x^2}}{(\sqrt{1+x^2})^2 - (\sqrt{1-x^2})^2} = \tan \alpha \\
&\Rightarrow \frac{1 - \sqrt{1-x^4}}{x^2} = \tan \alpha
\end{aligned}$$

$$1 - \sqrt{1-x^4} = x^2 \tan \alpha$$

$$(1 - x^2 \tan \alpha)^2 = 1 - x^4$$

$$1 - 2x^2 \tan \alpha + x^4 \tan^2 \alpha = 1 - x^4$$

$$x^4 - 2x^2 \tan \alpha + x^4 \tan^2 \alpha = 0$$

$$x^2 (x^2 - 2 \tan \alpha + x^2 \tan^2 \alpha) = 0$$

$$x^2 = \frac{2 \tan \alpha}{1 + \tan^2 \alpha}$$

$$x^2 = \frac{2 \tan \alpha}{\sec^2 \alpha}$$

$$x^2 = 2 \tan \alpha \cos^2 \alpha$$

$$x^2 = 2 \sin \alpha \cos \alpha = \sin 2\alpha$$

42. (a) Z has no maximum value

**Explanation:** Objective function is  $Z = -x + 2y$  .....(1).

The given constraints are :  $x \geq 3$ ,  $x + y \geq 5$ ,  $x + 2y \geq 6$ ,  $y \geq 0$ .

Corner points	$Z = -x + 2y$
D(6,0)	-6
A(4,1)	-2
B(3,2)	1

Here, the open half plane has points in common with the feasible region.

Therefore, Z has no maximum value.

43. (b)  $f(a) - a f'(a)$

**Explanation:**  $\lim_{x \rightarrow a} \frac{xf(a) - af(x)}{x - a}$

$$= \lim_{h \rightarrow 0} \frac{(a+h)f(a) - af(a+h)}{h} = \lim_{h \rightarrow 0} \left\{ \frac{hf(a)}{h} - \frac{af(a+h) - af(a)}{h} \right\} = f(a) - af'(a)$$

44. (c) AB is non-singular

**Explanation:** If A and B are non - singular then  $|AB| \neq 0$

= AB is non - singular matrix,

As  $|AB| = |A| |B|$

45. (d) reflexive and symmetric but not transitive

**Explanation:** Let S denote the set of all real numbers. Let R be a relation in S defined as  $a R b$  iff  $1 + ab > 0$ .

i. R is reflexive, Let a be any real number.

Then  $1 + aa = 1 + a^2 > 0$ , since  $a^2 \geq 0$ .

Thus  $a R a \forall a \in S$ . Therefore R is reflexive.

ii. R is symmetric. Let a, b be any two real numbers.

Then  $a R b \Rightarrow 1 + ab > 0 \Rightarrow 1 + ba > 0$  [ $\because ab = ba$ ]

$\therefore$  R is symmetric.

iii. R is not transitive. Consider three real number  $1, -\frac{1}{2}, -4$ .

We have

$$1 + 1 \left(-\frac{1}{2}\right) = \frac{1}{2} > 0$$

$$\therefore 1 R -\frac{1}{2}$$

$$\text{Further } 1 + \left(-\frac{1}{2}\right)(-4) = 3 > 0$$

$$\therefore -\frac{1}{2} R -4$$

But  $1 + 1(-4) = -3$  Which is not greater than 0. Therefore 1 is not R-related to -4.

Thus  $1 R -\frac{1}{2}, -\frac{1}{2} R -4$  and 1 is not R-related to -4.

$\therefore$  R is not transitive.

46. (a) 
$$\begin{matrix} & \begin{matrix} \text{Calories} & \text{Proteins} \end{matrix} \\ \begin{matrix} \text{Man} \\ \text{Woman} \\ \text{Children} \end{matrix} & \begin{bmatrix} 2400 & 45 \\ 1900 & 55 \\ 1800 & 33 \end{bmatrix} \end{matrix}$$

**Explanation:** Let F be the matrix representing the number of family members and R be the matrix representing the requirement of calories and proteins for each person. Then

$$F = \begin{matrix} & \begin{matrix} \text{Men} & \text{Women} & \text{Children} \end{matrix} \\ \begin{matrix} \text{Family A} \\ \text{Family B} \end{matrix} & \begin{bmatrix} 4 & 4 & 4 \\ 2 & 2 & 2 \end{bmatrix} \end{matrix}$$

$$R = \begin{matrix} & \begin{matrix} \text{Calories} & \text{Proteins} \end{matrix} \\ \begin{matrix} \text{Man} \\ \text{woman} \\ \text{Children} \end{matrix} & \begin{bmatrix} 2400 & 45 \\ 1900 & 55 \\ 1800 & 33 \end{bmatrix} \end{matrix}$$

47. **(d)** 24400

**Explanation:** The requirement of calories and proteins for each of the two families is given by the product matrix FR.

$$FR = \begin{bmatrix} 4 & 4 & 4 \\ 2 & 2 & 2 \end{bmatrix} \begin{bmatrix} 2400 & 45 \\ 1900 & 55 \\ 1800 & 33 \end{bmatrix}$$

$$= \begin{bmatrix} 4(2400 + 1900 + 1800) & 4(45 + 55 + 33) \\ 2(2400 + 1900 + 1800) & 2(45 + 55 + 33) \end{bmatrix}$$

$$FR = \begin{matrix} & \begin{matrix} \text{Calories} & \text{Proteins} \end{matrix} \\ \begin{bmatrix} 24400 & 532 \\ 12200 & 266 \end{bmatrix} & \begin{matrix} \text{Family A} \\ \text{Family B} \end{matrix} \end{matrix}$$

48. **(a)** 266 grams

**Explanation:** 266 grams

49. **(a)** A + B

**Explanation:** Since, AB = B ...(i) and BA = A ...(ii)

$$\therefore A^2 + B^2 = A \cdot A + B \cdot B$$

$$= A(BA) + B(AB) \text{ [using (i) and (ii)]}$$

$$= (AB)A + (BA)B \text{ [Associative law]}$$

$$= BA + AB \text{ [using (i) and (ii)]}$$

$$= A + B$$

50. **(b)** m = q

**Explanation:** A = (a<sub>ij</sub>)<sub>m × n</sub>, B = (b<sub>ij</sub>)<sub>n × p</sub>, C = (c<sub>ij</sub>)<sub>p × q</sub>

$$BC = (b_{ij})_{n \times p} \times (c_{ij})_{p \times q} = (d_{ij})_{n \times q}$$

$$(BC)A = (d_{ij})_{n \times q} \times (a_{ij})_{m \times n}$$

Hence, (BC)A is possible only when m = q